

# Recent Results on Hadron Spectroscopy from BESIII



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College of William and Mary  
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# Outline

- Confirmation of  $p\bar{p}$  mass threshold enhancement at BESIII
- Confirmation of X(1835) at BESIII
- Observation of  $h_c$
- Summary

# What can we do @BESIII

IJMP A V24 No 1 (2009) supp

- Light hadron spectroscopy
  - Full spectra: normal & exotic hadrons QCD
  - How quarks form a hadron? Non-pQCD
- Charm physics
  - CKM matrix elements SM & beyond
  - D  $\bar{D}$  mixing & CPV SM & beyond
- Charmonium physics
  - Spectroscopy & transition pQCD & non-pQCD
  - New states above open charm thresholds exotic hadrons ?
  - pQCD: rho pi puzzle a probe to non-pQCD or ?
- Tau physics & QCD
  - Precision measurement of the tau mass & R value
- Search for rare & forbidden decays

# Why can we do @BESIII

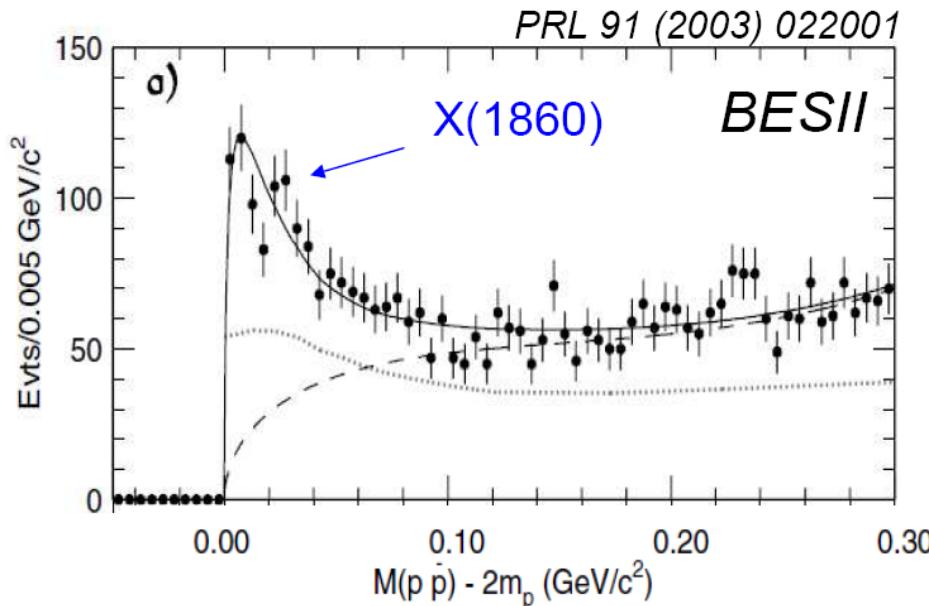
- Gluon rich
- Kinematics favorable
- Clean environment, no combinatoric background
- Important  $J^{PC}$  filter, and isospin filter

- High statistics: high luminosity machine
- Small systematic error: high quality detector.

a good platform to study precision charm physics & search for new physics.

# **Confirmation of $p\bar{p}$ mass threshold enhancement at BESIII**

# Observation of $p\bar{p}$ threshold enhancement in $J/\psi \rightarrow \gamma p\bar{p}$ @ BESII

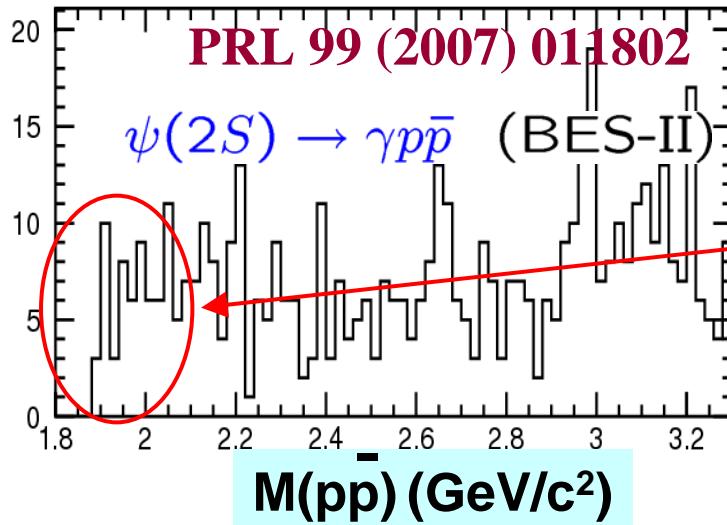
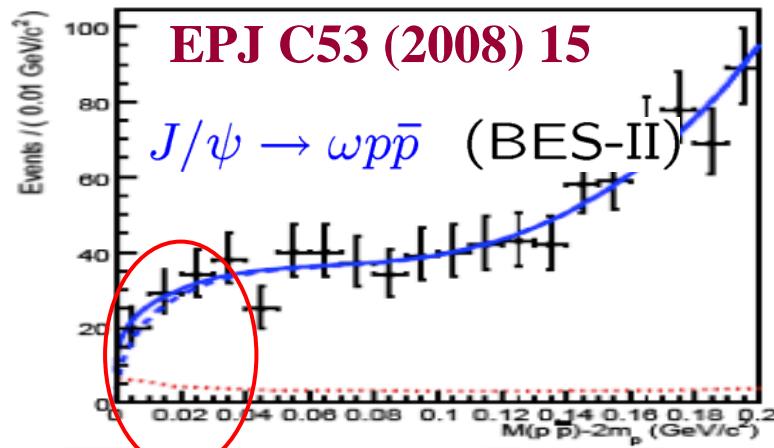
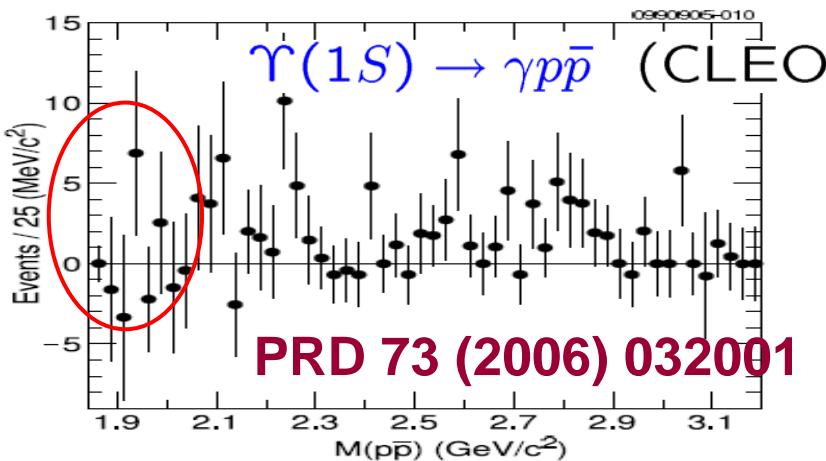


$M = 1859^{+3}_{-10} {}^{+5}_{-25} \text{ MeV}/c^2$   
 $\Gamma < 30 \text{ MeV}/c^2 (90\% \text{ CL})$

## theoretical speculation:

- $p\bar{p}$  bound state (baryonium)
- FSI effects
- .....

# Non-observation of X(1860) at $p\bar{p}$ mass threshold@ BESII



$M(p\bar{p}) - 2m_p$  (GeV/c<sup>2</sup>)

No significant signal of  
X(1860) found  
(only  $2\sigma$  statistic significance)

# $\bar{p}p$ mass threshold enhancement in $\psi' \rightarrow \pi^+ \pi^- J/\psi, J/\psi \rightarrow \gamma p\bar{p}$ @BESIII

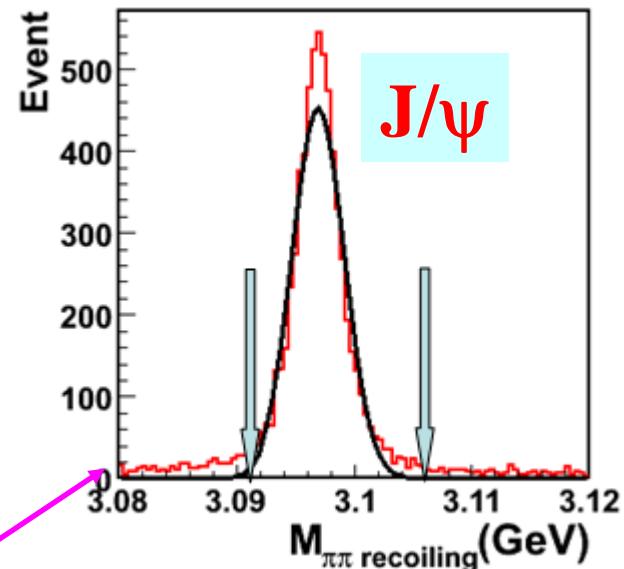
## Event selection

- Initial Selection Criteria:

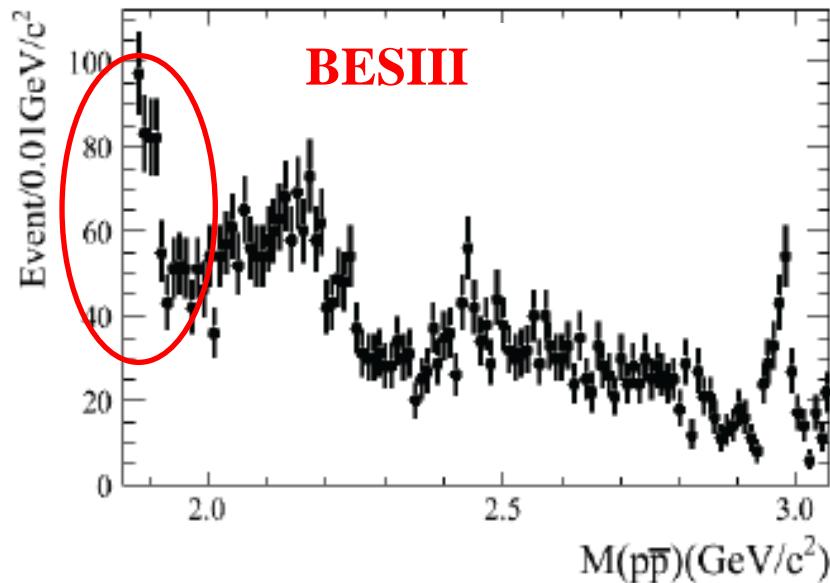
- $N_{\text{charged}} = 4, N_\gamma \geq 1$
- Particle ID:  $n_p = 1, n_{\bar{p}} = 1$
- $\chi^2_{4C}(\gamma\pi^+\pi^- p\bar{p}) < 100$

- Final Selection Criteria:

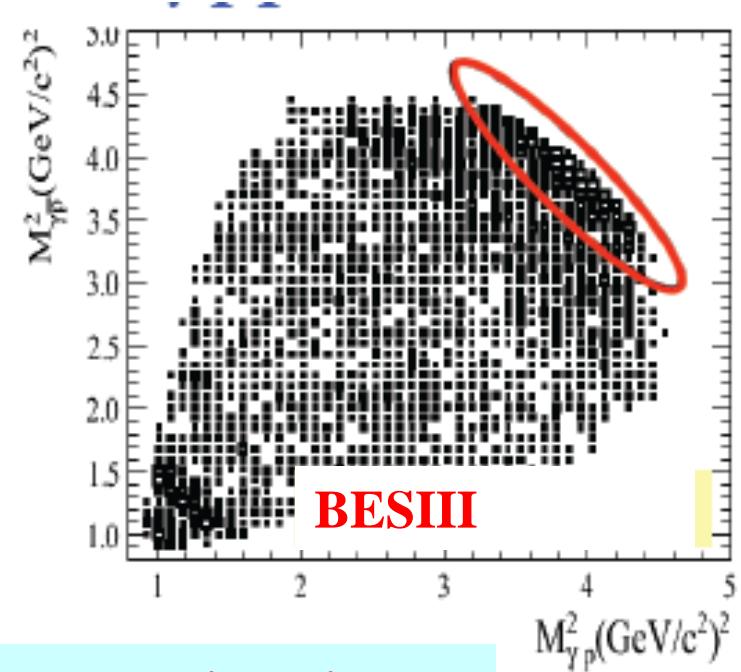
- Reconstruction of  $J/\Psi$ :  $|M_{\pi\pi\_recoiling} - M_{J/\psi}| < 6 \text{ MeV}$
- $|U_{miss}| < 0.04$
- $P_{t\gamma}^2 < 0.0005$
- $M_{\pi^+\pi^- p\bar{p}} < M_{\psi} + 15 \text{ MeV}$



# $p\bar{p}$ mass spectrum and Dalitz plot



BESIII

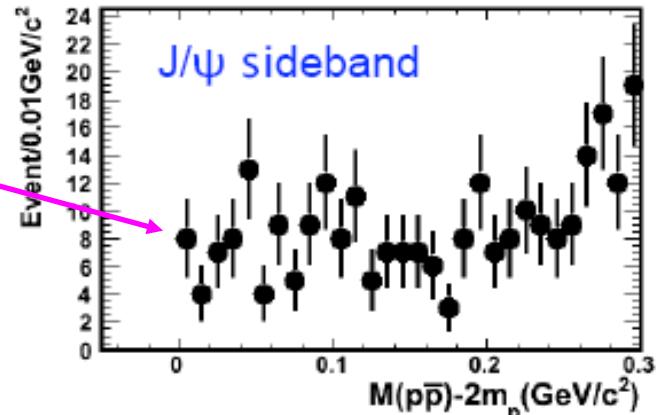


BESIII

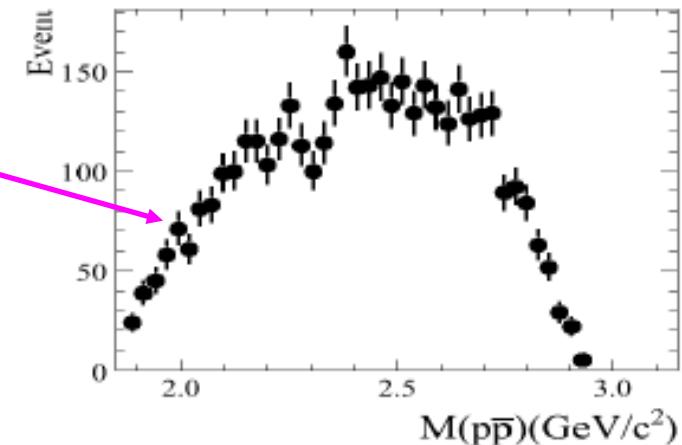
The mass threshold enhancement is evident  
in  $p\bar{p}$  mass spectrum

# Background study

- J/ $\psi$  sideband estimation
  - ~2%
- Inclusive MC sample
  - $\psi(2S) \rightarrow \pi\pi J / \psi(J/\psi \rightarrow \pi^0 p\bar{p})$



- Main background  
from  $\psi(2S) \rightarrow \pi\pi J / \psi(J/\psi \rightarrow \pi^0 p\bar{p})$



**No mass threshold enhancement observed from background**

# Mass spectrum fitting method

## ■ Fit function:

$$\psi' \rightarrow \pi^+ \pi^- J/\psi, J/\psi \rightarrow \gamma p\bar{p}$$

- signal: acceptance weighted S-wave BW

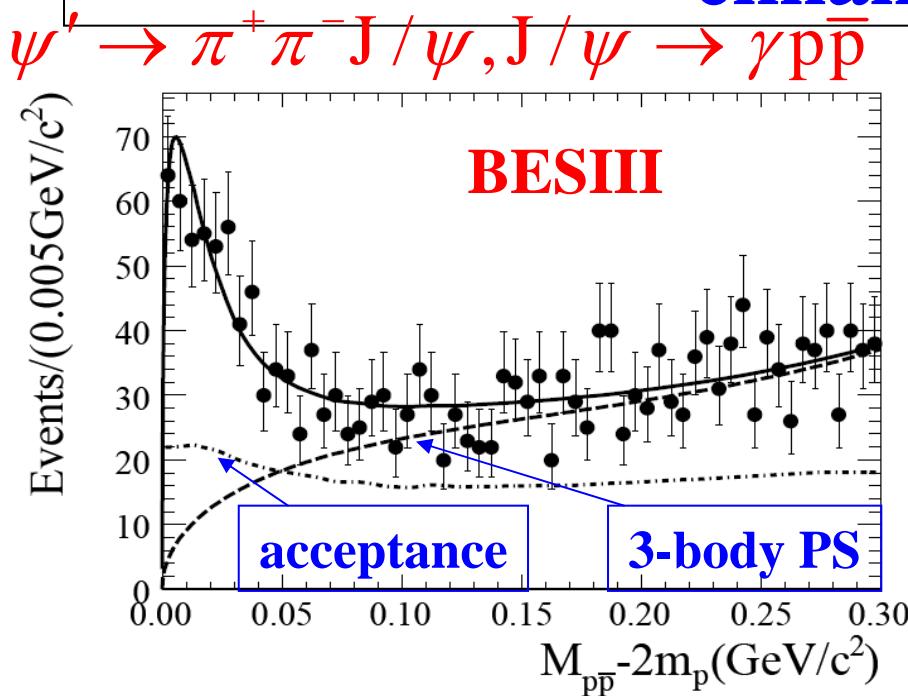
function:  $BW(M) \propto \frac{q^{(2l-1)} k^3}{(M^2 - M_0^2)^2 + M^2 \Gamma^2}$

- q : the proton momentum in cms of ppb
- k : the photon momentum
- $l$ : the ppb orbital angular momentum

- background shape:  $f_{bkg}(\delta) = \delta^{1/2} + a_1 \delta^{3/2} + a_2 \delta^{5/2}$

$a_1$  and  $a_2$  are obtain from uniform phase space MC sample

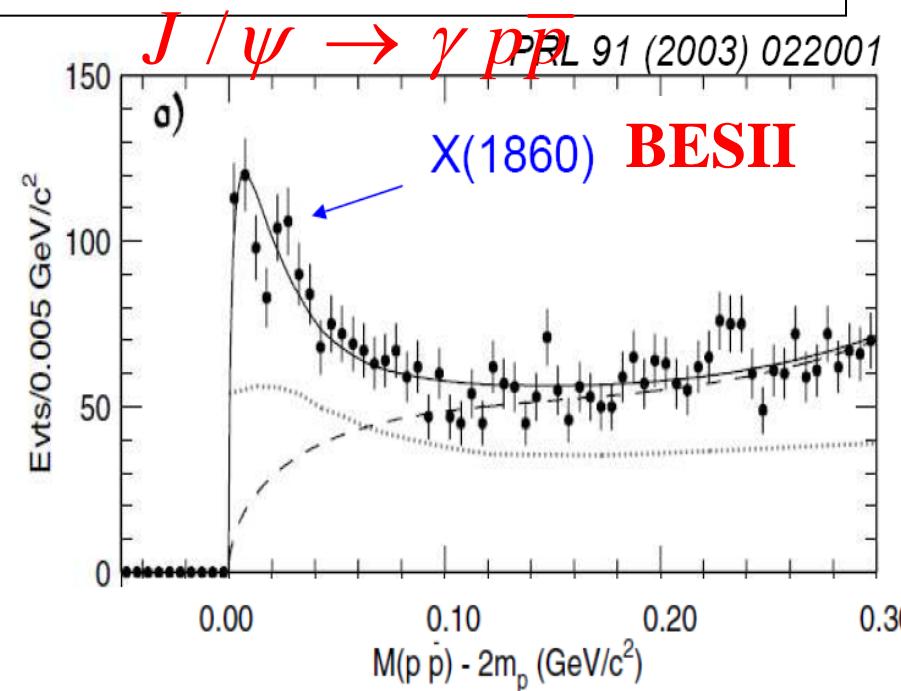
# confirmation of $p\bar{p}$ mass threshold enhancement



$M = 1865 \pm 5 \text{ MeV}/c^2$

$\Gamma < 33 \text{ MeV}/c^2$  (90% CL)

Published in  
Chinese Physics  
C 34(2010)421

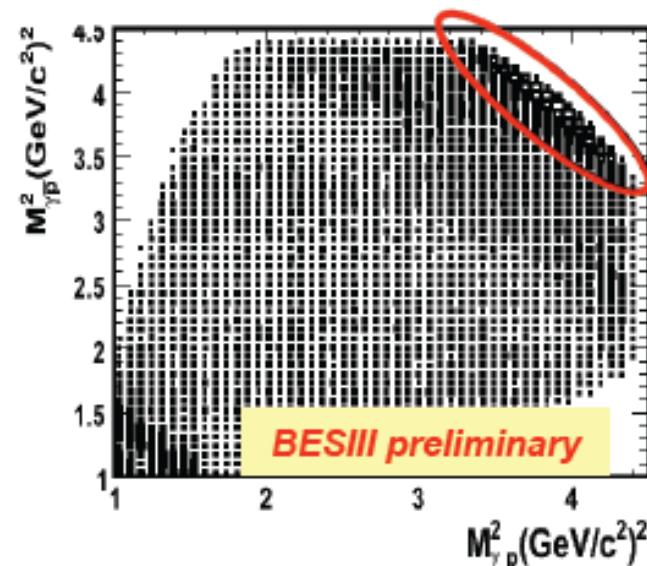
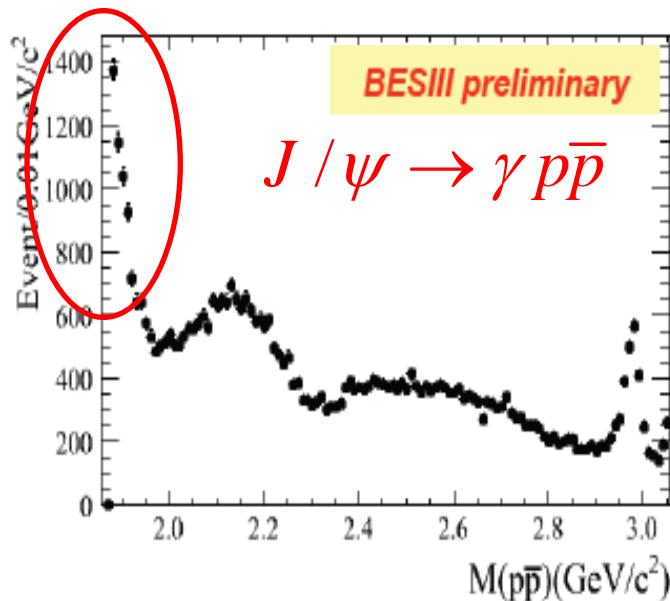


$M = 1859^{+3}_{-10} {}^{+5}_{-25} \text{ MeV}/c^2$

$\Gamma < 30 \text{ MeV}/c^2$  (90% CL)

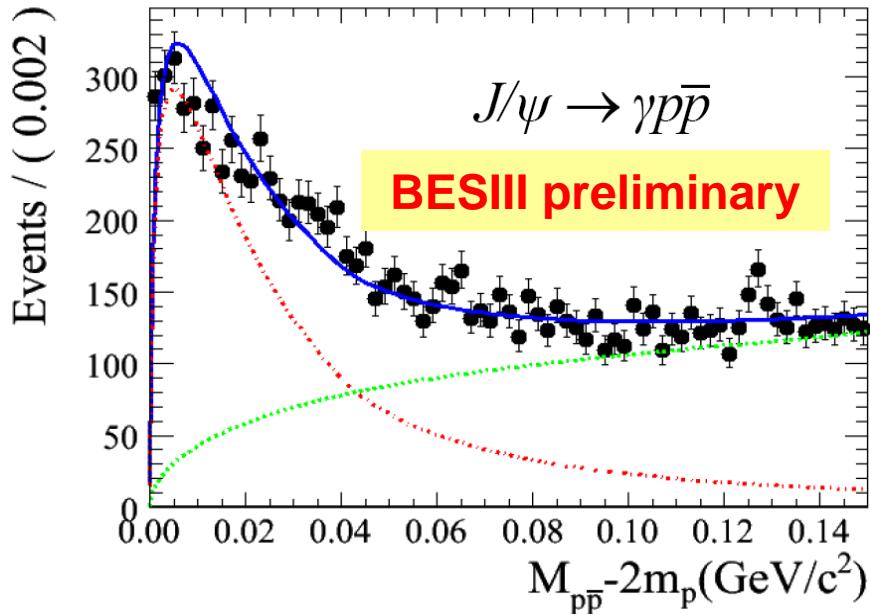
Confirmed at BESIII, the mass and width are consistent with those from BESII.

# pp mass threshold enhancement in $J/\psi \rightarrow \gamma pp$ @BESIII

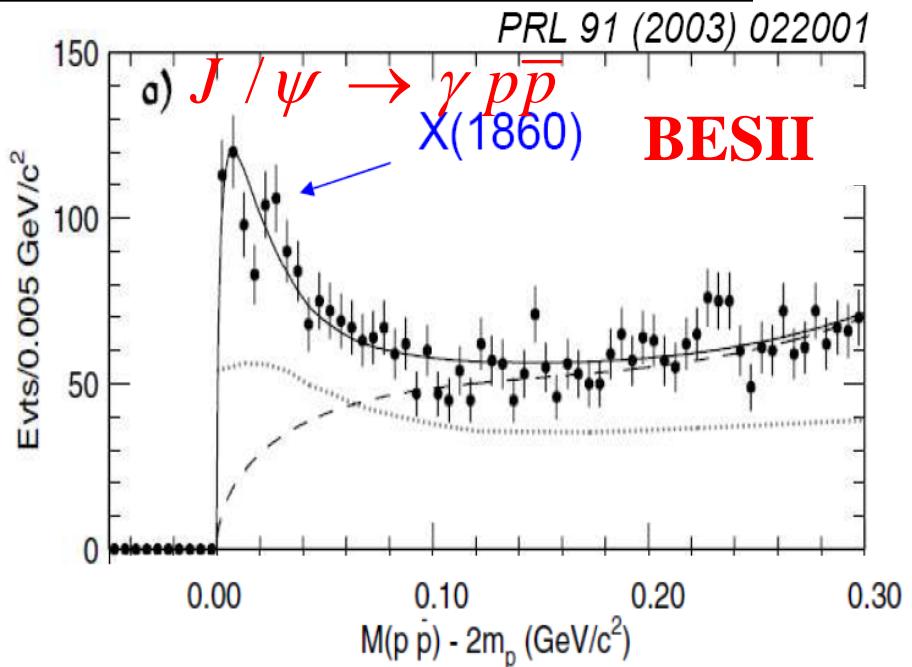


The mass threshold enhancement is evident  
in pp mass spectrum

# Fitting pp mass threshold enhancement



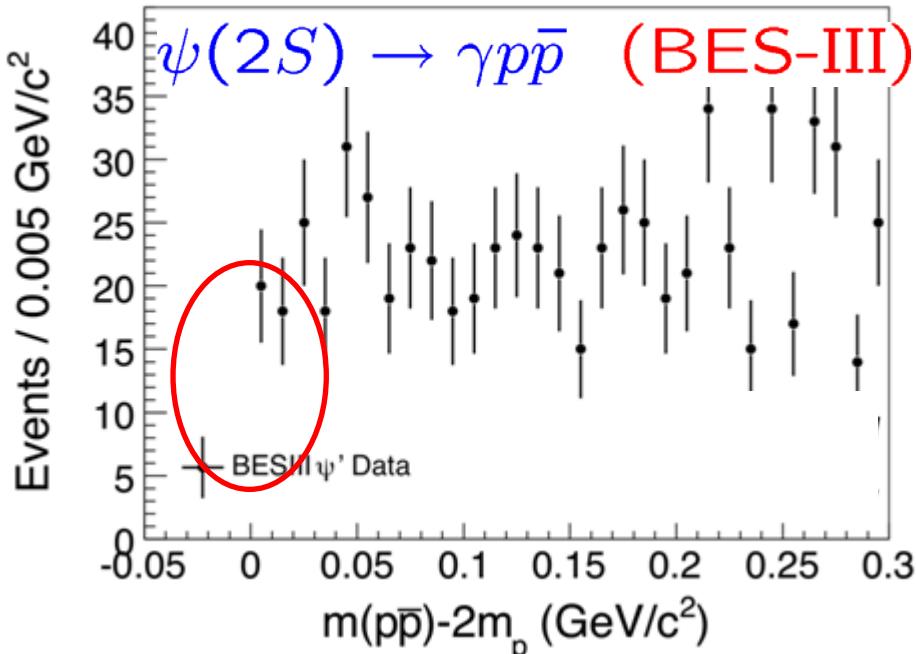
$M = 1861.6 \pm 0.8 \text{ MeV}/c^2$   
 $\Gamma < 8 \text{ MeV}/c^2 (90\% \text{ CL})$



$M = 1859^{+3}_{-10} {}^{+5}_{-25} \text{ MeV}/c^2$   
 $\Gamma < 30 \text{ MeV}/c^2 (90\% \text{ CL})$

Consistent results at BESIII

# Non-observation of mass enhancement in $\psi(2S) \rightarrow \gamma p\bar{p}$ @ BESIII

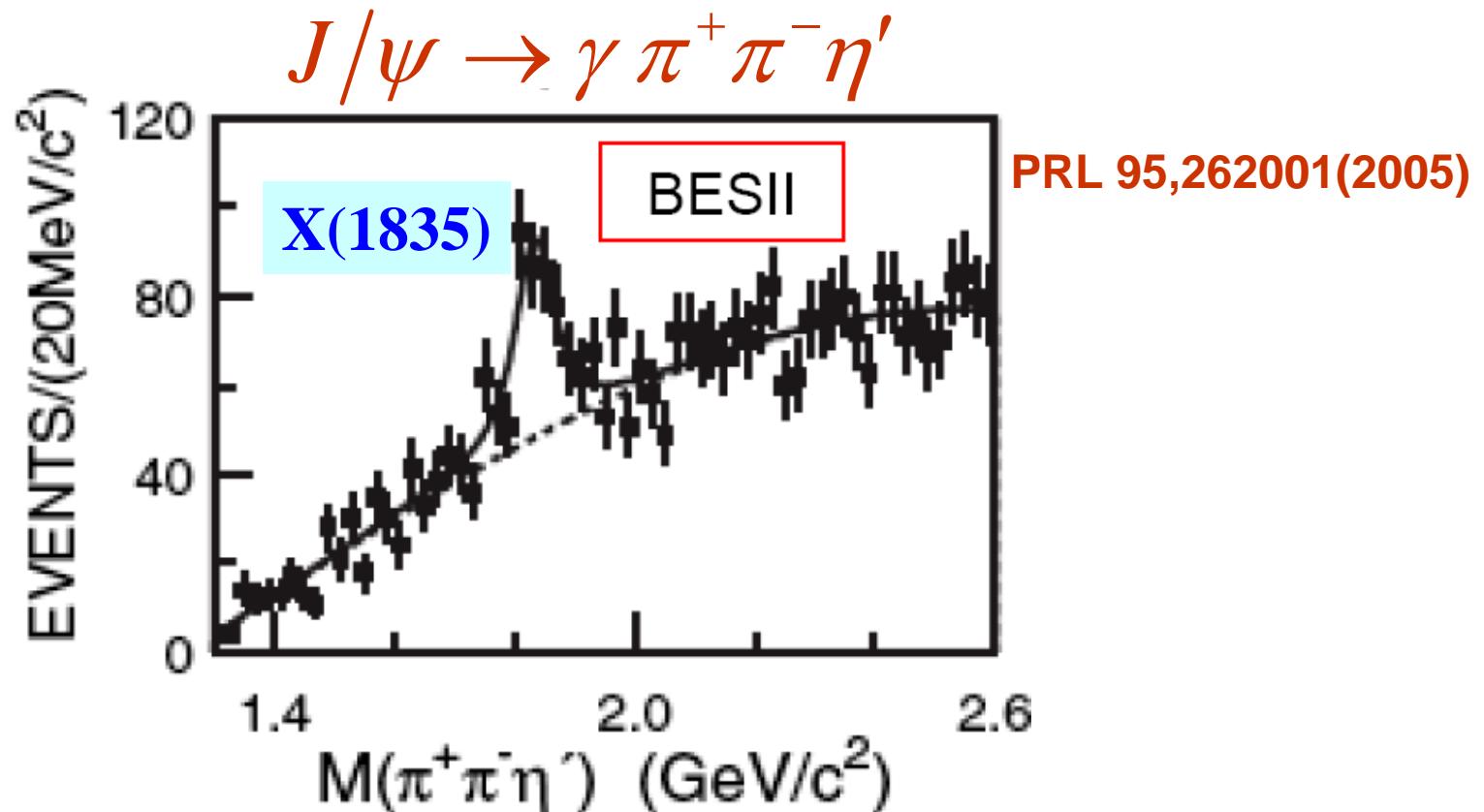


Confirmation of non-  
observation of  
enhancement in  
 $\psi(2S)$  channel!

⇒ pure FSI effect  
unlikely

# **Confirmation of X(1835) at BESIII**

# Observation of X(1835) @BESII



It's necessary to confirm X(1835) at BESIII  
with high statistic J/ $\psi$  data sample

# X(1835) in $J/\psi \rightarrow \gamma\eta'\pi^+\pi^-$ ( $\eta' \rightarrow \gamma\rho$ ) at BESIII

## Event selection

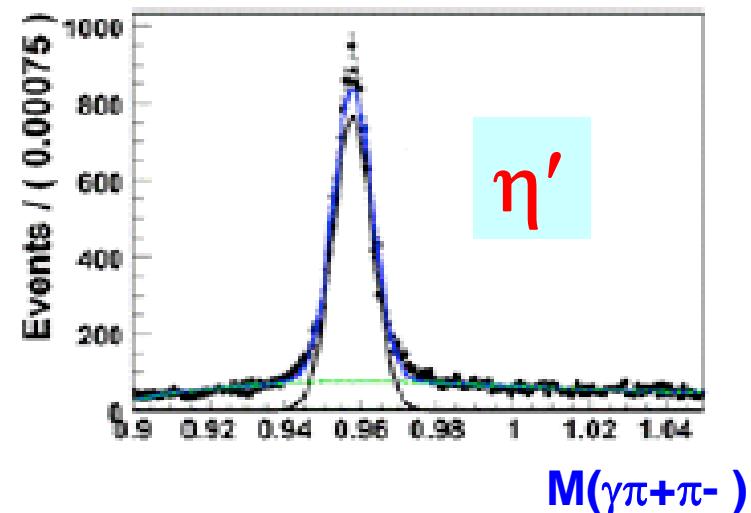
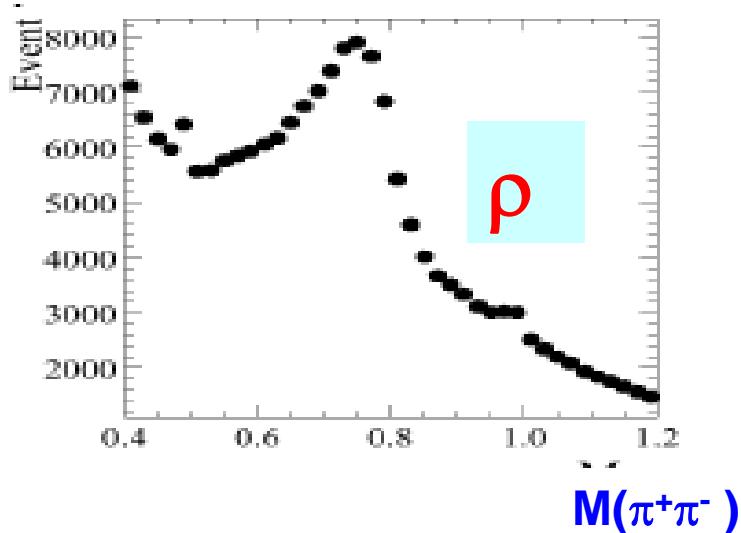
### ■ Initial selection criteria:

- $N_{\text{charged}} = 4$ ,  $N_\gamma \geq 2$
- $N_\pi > 2$
- Kinematic fit(4C):  
 $\chi^2_{4C}(\gamma\pi^+\pi^-\pi^+\pi^-) < 40$   
 $\chi^2_{4C}(\gamma\pi^+\pi^-\pi^+\pi^-) < \chi^2_{4C}(\gamma K^+K^-\pi^+\pi^-)$

### ■ Final selection criteria:

- Reduce background from  $\pi^0\pi^+\pi^-\pi^+\pi^-$ :  
 $|m_{\gamma\gamma} - m_\pi| < 0.04 GeV$   
 $|m_{\gamma\gamma} - m_\eta| < 0.03 GeV$   
 $0.72 GeV < m_{\gamma\gamma} < 0.82 GeV$

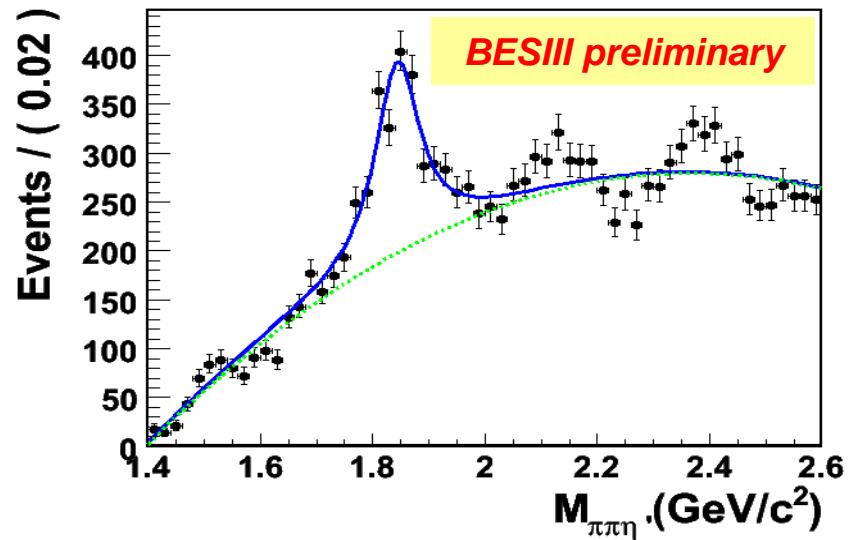
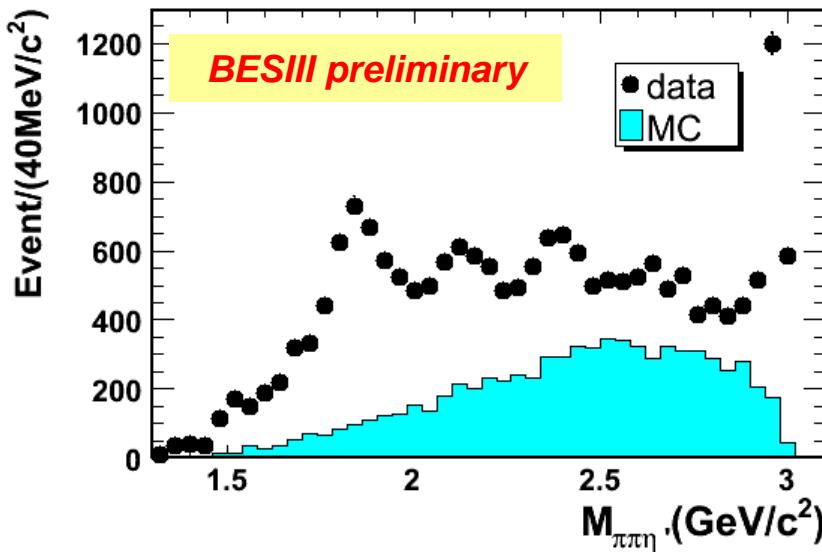
# X(1835) in $J/\psi \rightarrow \gamma\eta'\pi^+\pi^-$ ( $\eta' \rightarrow \gamma\rho$ ) @BESIII



$$|M(\pi^+\pi^-) - m_\rho| < 0.2 \text{ GeV}$$

$$|M(\gamma\pi^+\pi^-) - m_{\eta'}| < 0.018 \text{ GeV}$$

# Observation X(1835) in the mass spectrum of $\eta'\pi^+\pi^-$ ( $\eta' \rightarrow \gamma\rho$ )

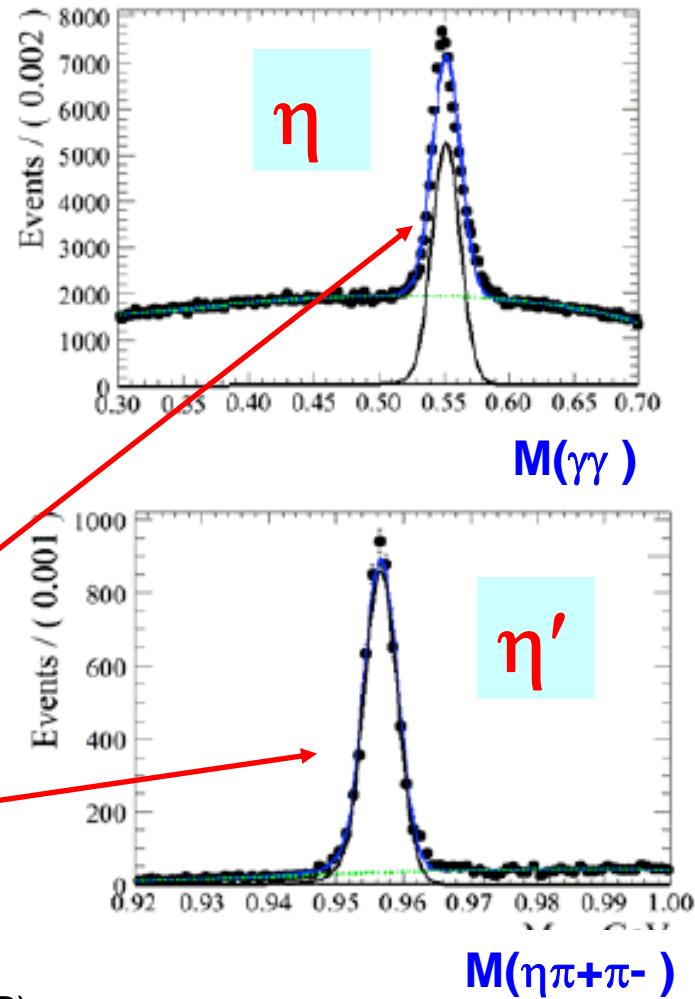


- Significant peak at  $M \sim 1835\text{MeV}$
- Statistical significance of X(1835) is about **18  $\sigma$  @ BESIII**  
**6  $\sigma$  @ BESII**

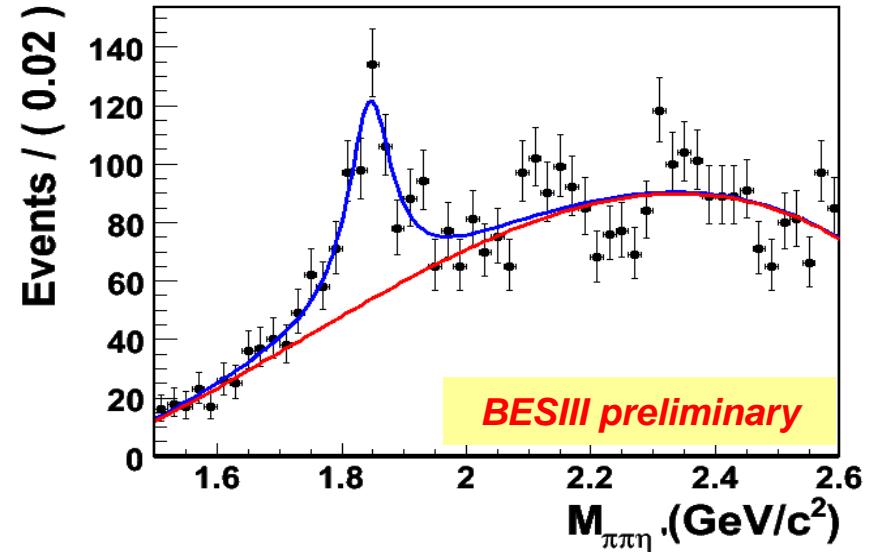
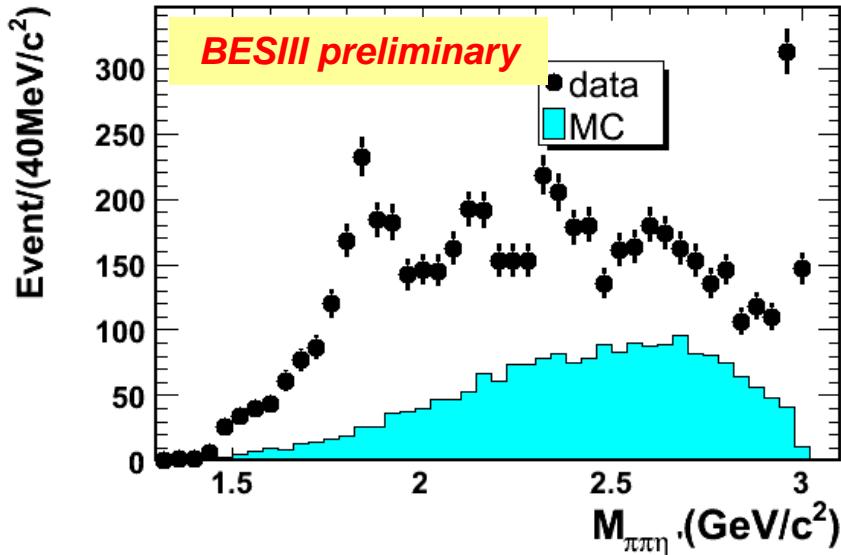
# X(1835) in $J/\psi \rightarrow \gamma\eta'\pi^+\pi^-$ ( $\eta' \rightarrow \eta\pi^+\pi^-$ ) @BESIII

## Event selection

- $N_{\text{charged}}=4, N_\gamma >= 3$
- $N_\pi > 2$
- Kinematic fit(4C,5C):  
 $\chi^2_{4C}(\gamma\gamma\pi^+\pi^-\pi^+\pi^-) < 40$   
 $\chi^2_{5C}(\gamma\eta\pi^+\pi^-\pi^+\pi^-) < 40$
- selection for  $\eta$  and  $\eta'$  signal:  
 $|M_{\gamma\gamma} - m_\eta| < 0.03 \text{ GeV}$   
 $|M_{\pi\pi\eta} - m_{\eta'}| < 0.01 \text{ GeV}$



# Observation of X(1835) in the mass sepctrum of $\eta'\pi^+\pi^-$ ( $\eta' \rightarrow \eta\pi^+\pi^-$ )



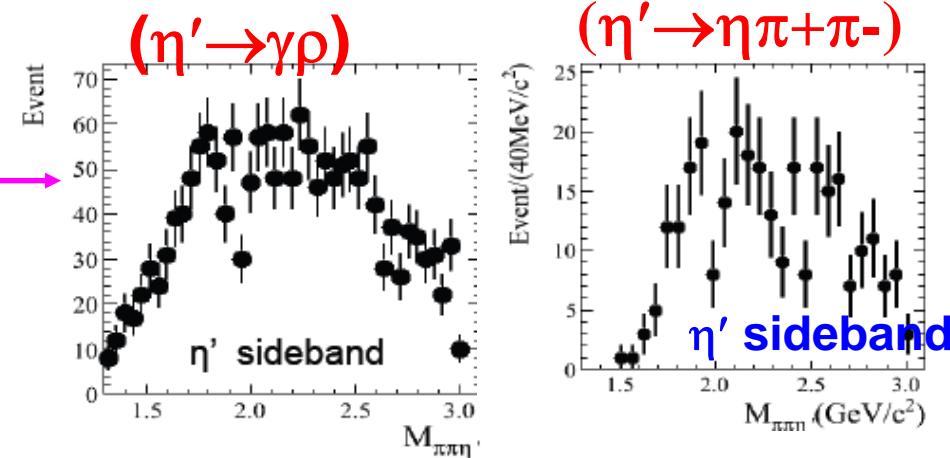
- Significant peak at  $M \sim 1835\text{MeV}$
- Statistic significance of X(1835) is **about  $9\sigma$  @BESIII**

# Background study for $J/\psi \rightarrow \gamma\eta'\pi^+\pi^-$

$(\eta' \rightarrow \gamma\rho \text{ & } \eta' \rightarrow \eta\pi^+\pi^-)$

- $\eta'$  sideband:

No clear peak at  $M \sim 1835 \text{ MeV}$



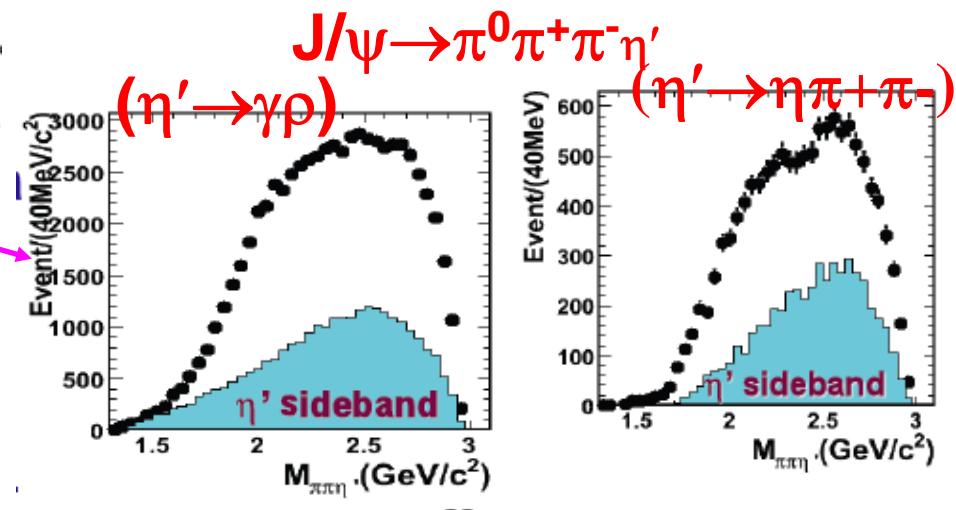
- Inclusive sample

main background channel:

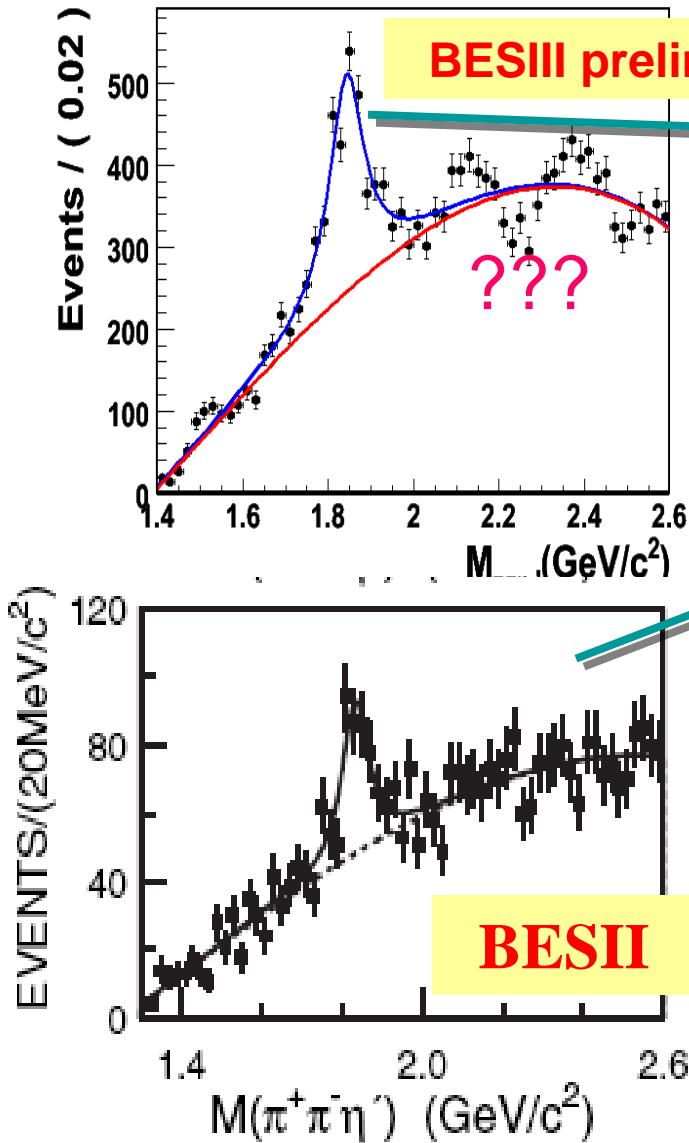
$$J/\psi \rightarrow \rho\pi\eta'$$

- Analysis of  $J/\psi \rightarrow \pi^0\pi^+\pi^-\eta'$  in data

No peak at  $M \sim 1835 \text{ MeV}$



# Combined mass spectrum of the two decay modes



**Statistic significance ~21σ@BESIII**

$$M = 1842.4 \pm 2.8(stat) MeV$$

$$\Gamma = 99.2 \pm 9.2(stat) MeV$$

**Statistic significance 7.7 σ@BESII**

$$M = 1833.7 \pm 6.1(stat) \pm 2.7(syst) MeV$$

$$\Gamma = 67.7 \pm 20.3(stat) \pm 7.7(syst) MeV$$

□ X(1835) is confirmed in BESIII and the significance increases as statistics increases

□ The possibility that there are two new resonances is under further study.

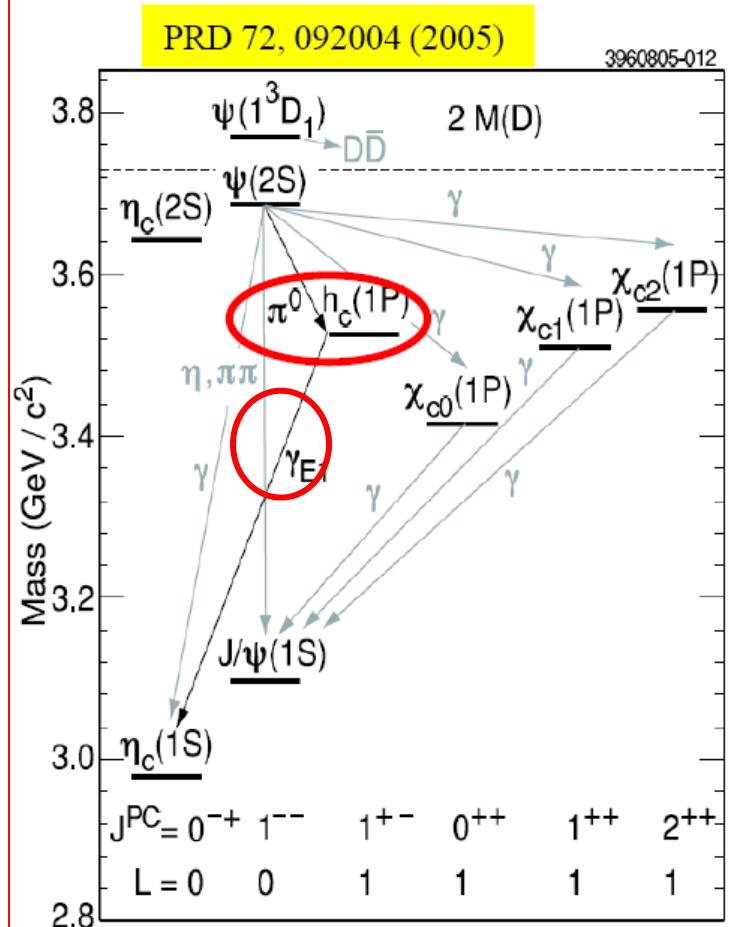
# **Observation of $h_c$**

# $h_c(1^P_1)$ in charmonium family

- Although the charmonium family has been studies for many years, knowledge is limited on the  $c\bar{c}$  P wave spin-singlet state  $h_c(1^P_1)$ .

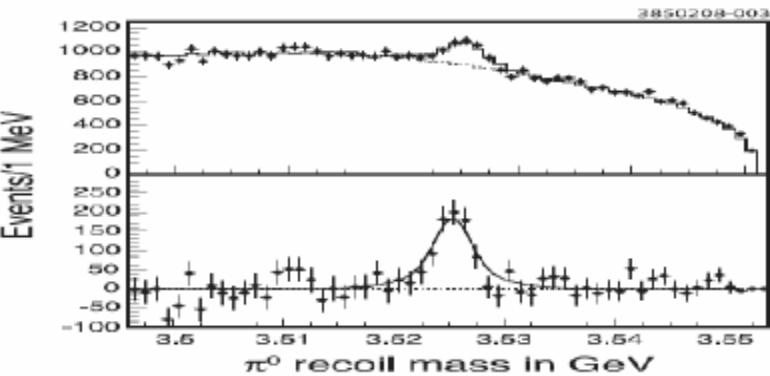
- In 2008,  $h_c$  was observed by CLEOc

- ✓ In the charmonium decays,  $h_c$  can only be observed in the process of  $\psi(2S) \rightarrow \pi^0 h_c$
- ✓ The main decay mode of  $h_c$  is the E1 transition  $h_c \rightarrow \gamma \eta_c$ .
- ✓  $M(h_c)$  is very close to  $M(1^3P) \approx 3525\text{MeV}$   
 $\Delta M_{hf} = M<1^1P_1> - M(1^3P) \sim 0.08 \pm 0.18 \pm 0.12\text{MeV}$  consistent to 1P hyperfine splitting of 0

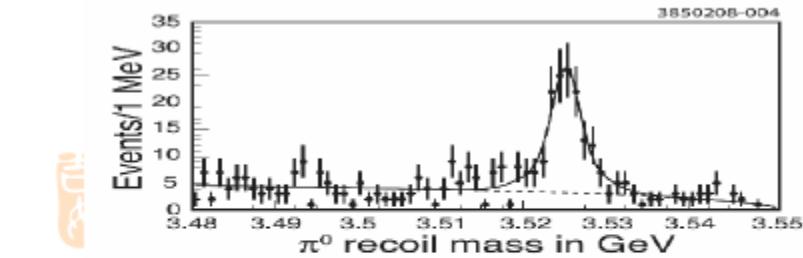


# $h_c$ @ CLEOc

CLEOc's Result –  $\psi' \rightarrow \pi^0 h_c$ ,  $h_c \rightarrow \gamma \eta_c$ , E1-tagged



CLEOc's Result –  $\psi' \rightarrow \pi^0 h_c$ ,  $h_c \rightarrow \gamma \eta_c$  exclusive



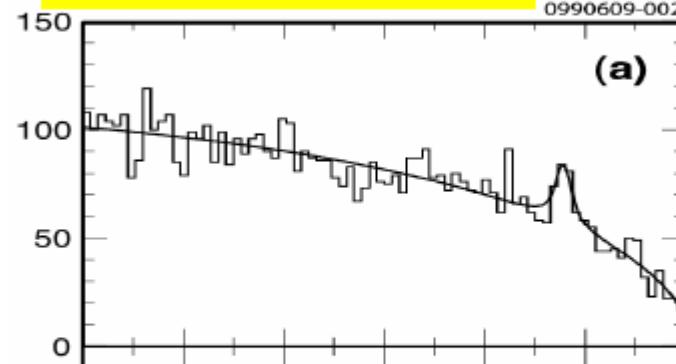
	Inclusive	Exclusive
Counts	$1146 \pm 118$	$136 \pm 14$
Significance	$10.0\sigma$	$13.2\sigma$
$M(h_c)$ (MeV)	$3525.35 \pm 0.23 \pm 0.15$	$3525.21 \pm 0.27 \pm 0.14$
$B_1 \times B_2 \times 10^4$	$4.22 \pm 0.44 \pm 0.52$	$4.15 \pm 0.48 \pm 0.77$

PRL101,182003(2008)

2 LHCb CMS

CLEOc's Result –  $\psi' \rightarrow \pi^0 h_c$ ,  $h_c \rightarrow 2(\pi^+\pi^-)\pi^0$

PRD80, 051106(2009).



Mode	efficiency (%)	Yield	$B_1 \times B_2 \times 10^5$
$\pi^+\pi^-\pi^0$	27.0	$1.6^{+5.7}_{-5.9}$	$< 0.19$
$2(\pi^+\pi^-)\pi^0$	18.8	$92^{+23}_{-22}$	$(1.88^{+0.48+0.47}_{-0.45-0.30})$
$3(\pi^+\pi^-)\pi^0$	11.5	$35 \pm 26$	$(1.2 \pm 0.9 \pm 0.3) (< 2.5)$

In previous experiments, the absolute branching ratios of  $\psi' \rightarrow \pi^0 h_c$  and  $h_c \rightarrow \gamma \eta_c$  have not been measured

# $h_c$ in E1-tagged $\psi(2S) \rightarrow \pi^0 h_c$ , $h_c \rightarrow \gamma \eta_c$ @BESIII

## Event selection

### Select inclusive $\pi^0$ ( $\psi' \rightarrow \pi^0 h_c$ )

- Photon polar angle:  $|\cos\theta| < 0.8$
- Photon energy:  $E_\gamma > 40\text{MeV}$
- Each photon belongs to only one  $\pi^0$
- $M_{\gamma\gamma} \in [0.12, 0.145]\text{GeV}/c^2$
- Do 1C fit for each  $\pi^0$  candidate (no cut on  $\chi^2$ )



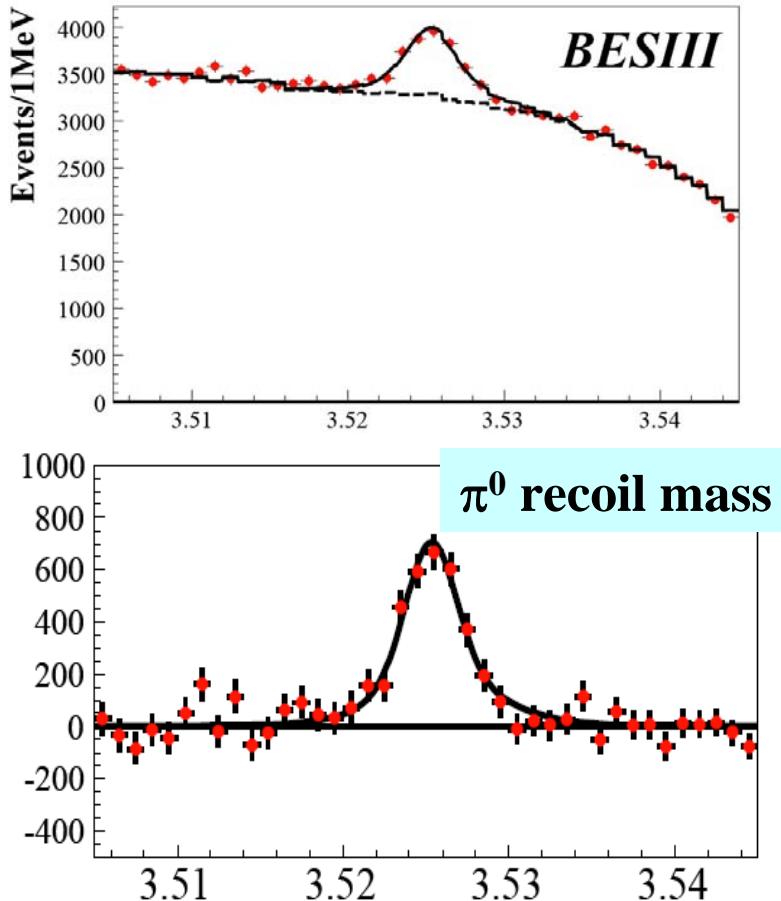
### Select E1-photon $\gamma$ to tag $h_c \rightarrow \gamma \eta_c$

- $450\text{MeV} < E_\gamma < 540\text{MeV}$
- Not belonging to  $\pi^0(0.10-0.145\text{GeV}/c^2)$  and  $\eta(0.53-0.56\text{GeV}/c^2)$

### Background veto

- $\pi^+ \pi^- J/\psi$  :  $|M^{\text{rec}}(\pi^+ \pi^-) - 3.097| > 0.007\text{GeV}/c^2$
- $\pi^0 \pi^0 J/\psi$  :  $|M^{\text{rec}}(\pi^0 \pi^0) - 3.097| > 0.03\text{GeV}/c^2$

# E1-tagged $\psi' \rightarrow \pi^0 h_c$ , $h_c \rightarrow \gamma \eta_c$



- A fit of double-Gaussian  $\otimes$  BW signal + E1-photon sideband background yield

**Significance=18.6 $\sigma$**

$$N(h_c) = 3679 \pm 319$$

$$M(h_c) = 3525.40 \pm 0.13 \text{ MeV}$$

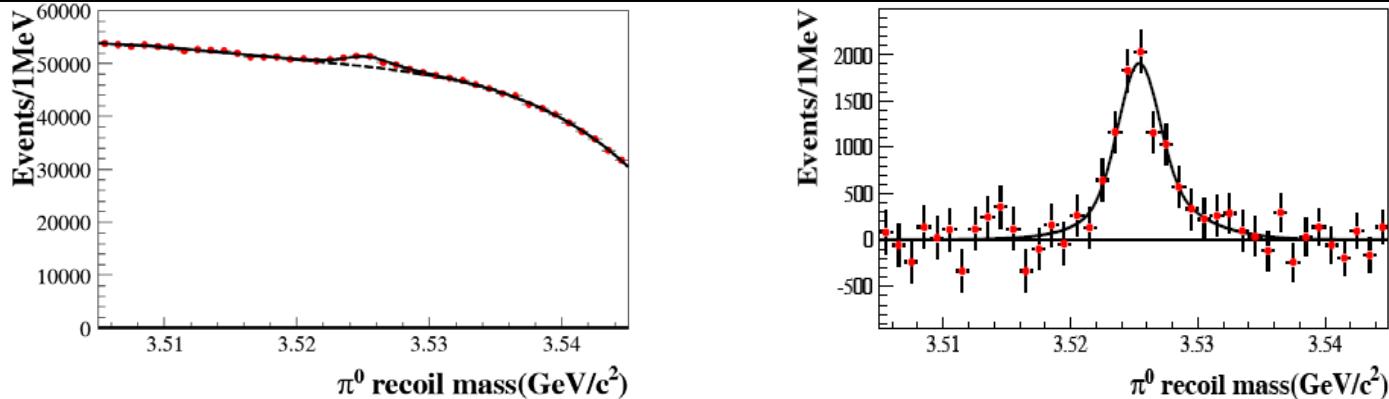
$$\Gamma(h_c) = 0.73 \pm 0.45 \text{ MeV}$$

$$\chi^2/\text{d.o.f} = 33.5/36$$

For the  
first time

$$\begin{aligned} \text{Br}(\psi' \rightarrow \pi^0 h_c) \times \text{Br}(h_c \rightarrow \gamma \eta_c) = \\ (4.58 \pm 0.40 \pm 0.50) \times 10^{-4} \end{aligned}$$

## $h_c$ in inclusive $\psi' \rightarrow \pi^0 h_c$ (un>tagged E1- photon)



- Select inclusive  $\pi^0$  ( $\psi' \rightarrow \pi^0 h_c$ )
- Untagged E1-photon
- A fit of D-Gaussian  $\otimes$  BW signal + 4<sup>th</sup> Poly. BG yeild.  
mass and width is fixed as tagged measurement

Combined with tagged results,  
we measured for the first time :

- $\text{Br}(\psi' \rightarrow \pi^0 h_c) = (8.4 \pm 1.3 \pm 1.0) \times 10^{-4}$  (2010)
- $\text{Br}(h_c \rightarrow \gamma \eta_c) = (54.3 \pm 6.7 \pm 5.2)\%$

BES Collaboration,  
PRL 104, 132002

# Summary for $h_c$ analysis

	BESIII	CLEOc	theoretical prediction
$\text{Br}(\psi' \rightarrow \pi^0 h_c)$ $\times \text{Br}(h_c \rightarrow \gamma \eta_c)$ [ $10^{-4}$ ]	$4.58 \pm 0.40 \pm 0.50$	$4.19 \pm 0.32 \pm 0.45$	-
$M [\text{MeV}/c^2]$	$3525.40 \pm 0.13 \pm 0.18$	$3525.80 \pm 0.19 \pm 0.12$	-
$\Gamma [\text{MeV}]$	$0.73 \pm 0.45 \pm 0.28$ $<1.44 @ 90\% \text{CL}$	-	1.1 (NRQCD) Kuang 0.51 (PQCD) Kuang
$\Delta M_{hf}(1P)$ [ $\text{MeV}/c^2$ ]	$0.10 \pm 0.13 \pm 0.18$	$0.08 \pm 0.18 \pm 0.12$	
$\text{Br}(\psi' \rightarrow \pi^0 h_c)$ [ $10^{-4}$ ]	$8.4 \pm 1.3 \pm 1.0$	-	4 - 13
$\text{Br}(h_c \rightarrow \gamma \eta_c)$	$54.3 \pm 6.7 \pm 5.2$	-	41 (NRQCD) Kuang 88 (PQCD) Kuang 38 Godfrey, Rosner

CLEO-c Collaboration, Phys.Rev.Lett.101:182003,2008

2010-5-31 BES Collaboration, PRL 104, 132002 (2010)

Fang Liu(IHEP)  
Theoretical predictions: PRD65, 094024 (2002) & PRD 66, 014012 (2002).

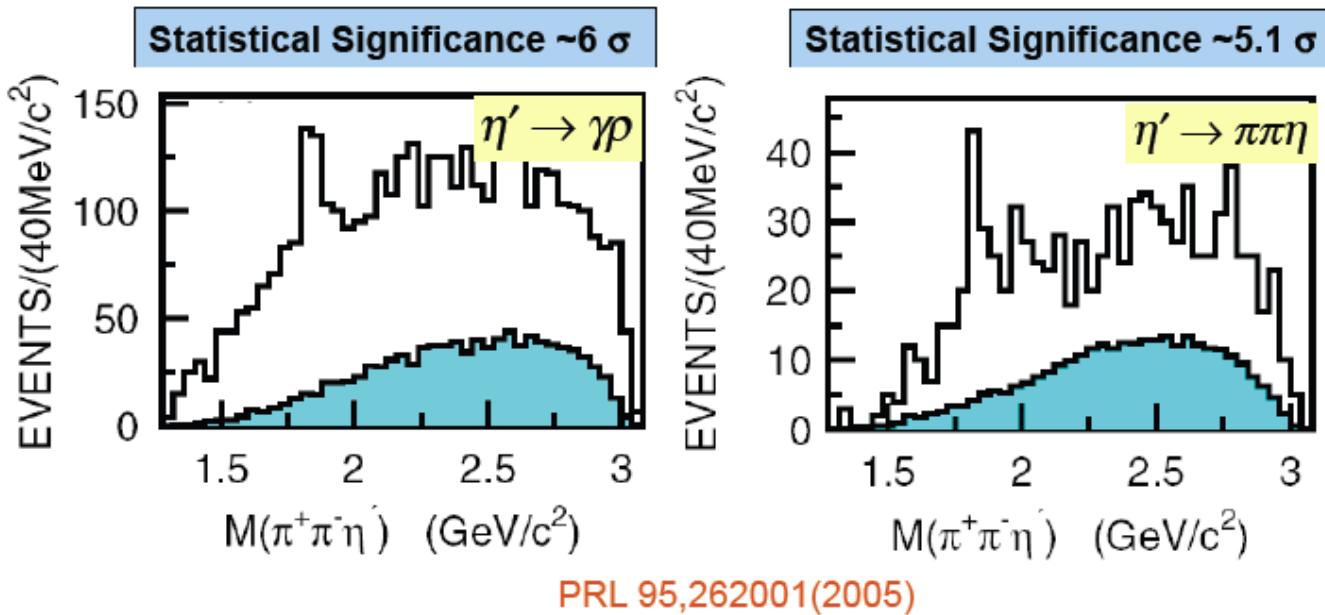
# Summary

- $p\bar{p}$  mass threshold enhancement has been confirmed in  $\psi' \rightarrow \pi^+ \pi^- J/\psi (J/\psi \rightarrow \gamma p\bar{p})$  and  $J/\psi \rightarrow \gamma p\bar{p}$  and no significance mass enhancement is observed in  $\psi' \rightarrow \gamma p\bar{p}$  at BESIII
- X(1835) is confirmed in the two decay modes ( $\eta' \rightarrow \gamma \rho$  and  $\eta' \rightarrow \eta \pi^+ \pi^-$ ) for  $J/\psi \rightarrow \gamma \eta' \pi^+ \pi^-$
- From inclusive and E1-tagged analysis, we observed  $h_c$  and measured
  - $\Gamma(h_c) = 0.89 \pm 0.57 \pm 0.23 \text{ MeV}$
  - $B_1(\psi' \rightarrow \pi^0 h_c) = (8.42 \pm 1.29(\text{stat.})) \times 10^{-4}$  and
  - $B_2(h_c \rightarrow \gamma \eta_c) = (55.7 \pm 6.3(\text{stat.}))\%$  for the first time.
- More Exciting results are expected in the coming years.

# Back up

# Back up

## Observation of X(1835) in $J/\psi \rightarrow \gamma \pi^+ \pi^- \eta'$ at BESII



# speculation for X(18\*\*)

- The strong and narrow  $p\bar{p}$  mass threshold enhancement has only been observed in  $J/\psi$  radiative decay, not in any other place so far.
- Any model trying to interpret the mass threshold enhancement should also answer why it is not observed in other places, especially in  $\psi(2S)$  and  $\Upsilon(1S)$  radiative decays as well as in  $J/\psi \rightarrow \omega p\bar{p}$  process.
  - ✧ Whether X(1860) and X(1835) are the same resonance, still needs further study.

# $h_c$ : spin-spin interaction

The cc singlet state  $h_c$  was predicted by theory long time ago.

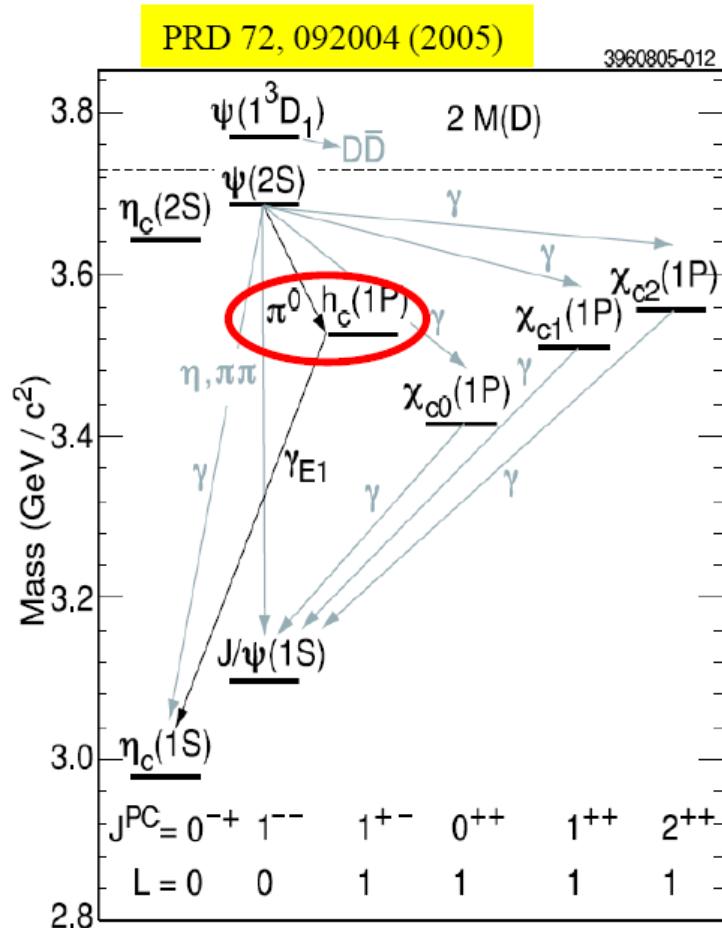
In 2008,  $h_c$  was observed by CLEO\_c in charmonium decays

$h_c$  can only be observed in the process of  $\gamma(2S) \rightarrow p0h_c$

the main decay mode of  $h_c$ :  
the E1 transition  $h_c \rightarrow \gamma h_c$ .

- Test of QCD and potential model  
spin-spin-interaction tells us:

$$\Delta M_{hf}(1P) = m(h_c) - \frac{1}{9} (m(\chi_{c0}) + 3m(\chi_{c1}) + 5m(\chi_{c2}))$$



# $h_c$ in CIEOc and E853

data were done. In the *inclusive analysis*  $h_c$  decays were identified by loose constraints on either the energy of the electric dipole (E1) photon from  $h_c$  decay, or the mass of  $\eta_c$ . In the *exclusive analysis* no constraint was placed on  $E(\gamma)$ . Instead,  $\eta_c$  events were reconstructed in seven different hadronic decay channels of  $\eta_c$ . The combined significance level of the  $h_c$  observation was  $>6\sigma$ , and the quoted mass was  $M(h_c) = 3524.4 \pm 0.6 \pm 0.4$  MeV.

The Fermilab E835 measurement [3] made scans of antiproton energy for the reaction,  $\bar{p}p \rightarrow h_c \rightarrow \gamma\eta_c, \eta_c \rightarrow \gamma\gamma$ . The results from the year 1997 scan and the year 2000 scan were combined to obtain  $M(h_c) = 3525.8 \pm 0.2 \pm 0.2$  MeV. The significance level of  $h_c$  observation was  $\sim 3\sigma$ . No evidence was found for  $h_c$  in the previously reported reaction  $\bar{p}p \rightarrow h_c \rightarrow \pi^0 J/\psi$  [5].

# Event selection for the inclusive $\pi^0$ and E1-tagged analysis

- ◆ Inclusive analysis of  $\psi(2S) \rightarrow \pi^0 h_c$ 
  - Identify the  $h_c$  signal by searching for an enhancement in the inclusive recoiling mass spectrum of  $\pi^0$
- ◆ E1-tagged analysis of  $\psi(2S) \rightarrow \pi^0 h_c, h_c \rightarrow \gamma \eta_c$ 
  - Tag the E1 photon ( $\sim 503$  MeV) emitted in  $h_c \rightarrow \gamma_{E1} \eta_c$ . No further constraints on the final states of the  $\eta_c$  are imposed. The  $h_c$  signal in  $\pi^0$  recoil mass spectrum will be improved significantly.
- ◆ Exclusive analysis of  $\psi(2S) \rightarrow \pi^0 h_c, h_c \rightarrow \gamma \eta_c$ 
  - Fully reconstruct the exclusive final states of  $\eta_c$

# Event selection for the inclusive $\pi^0$ and E1-tagged analysis

## ◆ Good charged track

- IP region:  $|R_{xy}| \leq 1\text{cm}$ ,  $|Rz| \leq 10\text{cm}$
- Momentum:  $p < 2.0\text{GeV}$
- Polar angle:  $|\cos\theta| < 0.93$
- $N_{\text{charge}} \geq 2$ ,  $N_{\text{good}} \geq 1$

## ◆ Good photon

- $|\cos\theta| < 0.8$ :  $E_\gamma > 25\text{MeV}$
- $0.84 < |\cos\theta| < 0.92$ :  $E_\gamma > 50\text{MeV}$
- Angle between charged track and neutral track:  $D_{\text{ang}} < 20^\circ$
- EMC time:  $0 \leq t \leq 14$  ( $\times 50\text{ns}$ )

# Event selection for the inclusive $\pi^0$ and E1-tagged analysis

## ◆ signal $\pi^0$ candidate selection

- Photon polar angle:  $|\cos\theta| < 0.8$
- Photon energy:  $E_\gamma > 40 \text{ MeV}$
- Each photon belongs to only one  $\pi^0$
- $M_{\gamma\gamma} \in [0.12, 0.145] \text{ GeV}/c^2$
- Do 1C fit for each  $\pi^0$  candidate (no cut on  $\chi^2$ )

## ◆ Tag E1 photon in $h_c \rightarrow \gamma_{E1} \eta_c$

- $450 \text{ MeV} < E_\gamma < 540 \text{ MeV}$
- Not belonging to  $\pi^0$  ( $0.10 - 0.145 \text{ GeV}/c^2$ ) and  $\eta$  ( $0.53 - 0.56 \text{ GeV}/c^2$ )

## ◆ Background Veto

- $\pi^+ \pi^- J/\psi$  :  $|M^{\text{rec}}(\pi^+ \pi^-) - 3.097| > 0.007 \text{ GeV}/c^2$
- $\pi^0 \pi^0 J/\psi$  :  $|M^{\text{rec}}(\pi^0 \pi^0) - 3.097| > 0.03 \text{ GeV}/c^2$

# Systematic error for $h_c$ analysis

source	$M(h_c)$ (MeV/ $c^2$ )	$\Gamma(h_c)$ (MeV)	$\mathcal{B}_1(10^{-4})$	$\mathcal{B}_1 \times \mathcal{B}_2(10^{-4})$	$\mathcal{B}_2(\%)$
Background shape and fit range	0.11	0.23	0.4	0.22	4.4
Energy scale, position reconstruction and 1-C fit	0.13	0.06	0.5	0.10	2.1
Energy resolution	0.00	0.15	0.2	0.03	1.0
Background veto	0.05	0.03	0.0	0.03	0.3
$\pi^0$ efficiency	0.00	0.00	0.3	0.14	0.0
$E1$ photon efficiency	0.00	0.00	0.0	0.10	1.2
Number of $\pi^0$	0.00	0.00	0.6	0.35	0.6
Number of charged tracks	0.00	0.00	0.1	0.06	0.1
$N(\psi')$	0.00	0.00	0.4	0.19	0.0
$M(\psi')$	0.03	0.02	0.0	0.00	0.0
$M(\eta_c)$ and $\Gamma(\eta_c)$	0.00	0.00	0.0	0.01	0.3
Total systematic error	0.18	0.28	1.0	0.50	5.2

The CLEO average mass in Eq. (6) leads to

$$\Delta M_{hf}(1P) = +0.08 \pm 0.18(\text{stat.}) \pm 0.12(\text{syst.})\text{MeV}.$$

These results are consistent with the lowest order expectation of  $1P$  hyperfine splitting being zero. We notice that the triplet mass used above was obtained as  $\langle M(^3P_J) \rangle = [M(^3P_0) + 3M(^3P_1) + 5M(^3P_2)]/9$ , which is the evaluation of  $M(^3P)$  in the lowest order, when the spin-orbit splitting is perturbatively small. It has been pointed out [4] that with  $[M(^3P_2) - M(^3P_0)] \approx 140$  MeV, the validity of the perturbative determination of  $M(^3P)$  is questionable. Indeed, the perturbative prediction that  $M(^3P_1) - M(^3P_0) = \frac{5}{2}[M(^3P_2) - M(^3P_1)] = 113.9 \pm 0.3$  MeV disagrees with the experimental result,  $95.9 \pm 0.4$  MeV, by 18 MeV. This necessarily implies that the true  $M(^3P)$  is different from the centroid value  $\langle M(^3P_J) \rangle$ . Since  $\Delta M_{hf}(1P)$  is expected to be small ( $\sim$  few MeV), if not identically zero, it is important that higher order effects should be taken into account in deducing  $M(^3P)$  from the known masses of  $^3P_J$  states [4], so that a true measure of  $\Delta M_{hf}(1P)$  can be obtained. Only then can the present measurement of  $M(h_c)$  be used to distinguish between the different potential model calculations, whose predictions for  $\Delta M_{hf}(1P)$  vary over a large range because of the different assumptions they make about relativistic effects, the Lorentz nature of the confinement potential, and smearing of the spin-spin contact potential [12]. Although the presently available lattice calculations do not have the required precision [13], it may be expected that future unquenched lattice calculations will resolve these problems.

## Hyperfine mass splitting